# PROPERTIES OF HIGH-TEMPERATURE SUPERCONDUCTORS IN A TWO-BAND MODEL WITH THE DOPING-DEPENDENT ELECTRON SPECTRUM

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Abstract. A simple model of interband superconductivity, incorporating a basic band and a doping created one (constant total number of states), is considered, keeping in mind the two-component scenario of high- $T_{\rm c}$  superconductivity. The dependences of  $T_{\rm c}$ , its isotope exponent, superconductivity gaps, etc. on doping are calculated using an illustrative set of parameters. The observed types of behaviour are reproduced. Diminishing gap ratios with hole doping have been found. In the one-particle excitation spectrum the peak—dip—hump type complex can be identified. In spite of crude approximations the model reflects, in general, the experimental findings on high- $T_{\rm c}$  cuprates. Two-band models will remain a channel for looking for the high- $T_{\rm c}$  mechanism.

**Key words:** high-temperature superconductivity, two-band models, doping, gaps.

#### 1. INTRODUCTION

The superconductivity mechanism of high- $T_{\rm c}$  cuprate systems is still under debate and a number of different theories are being developed. The present work concentrates on one of the possible approaches.

Numerous results point to the multicomponent nature of the order parameter, several elementary excitation gaps, two pairing scales, participation of several electronic bands or subsystems, etc. in the basic physics of cuprate superconductors (e.g.  $[^{1-5}]$ ). This trend is nowadays concentrated in the "two-component scenario" of high- $T_{\rm c}$  superconductivity  $[^{6-11}]$ . It establishes the participation of two different electronic subsystems one of which is of basic itinerant, the other of quasilocalized nature, the latter being associated with the doping treatment.

These subsystems (bands) can be presumably connected with doping-induced stripe-ordering phase separation in the superconductivity playground  $\text{CuO}_2$  planes [ $^{12-17}$ ]. This self-organization process in the two-dimensional electron subsystem generates undistorted material stripes alternating with doping charge bearing distorted regions. This charge and spin (static or fluctuating) inhomogeneity is considered as a key phenomenon in the physics of superconducting cuprates [ $^{18}$ ].

In connection with the two-component scenario a hole-type itinerant band and a narrow doping-created distribution of (localized; percolating) states are usually mentioned. It seems natural to describe the superconductivity mechanism in such a situation by two-band models  $[^{19-21}]$ . A number of various two-band schemes have been developed using interacting partners traced back to different origins. Particularly, characteristic trends of  $T_c$ , its isotope effect exponent and some properties of gaps were obtained in the scheme of two overlapping bands in papers  $[^{21-27}]$ .

Only few recent approaches use a doping-dependent electron spectrum or connect it with stripening. A multiband description of the cuprate high- $T_{\rm c}$  phenomenon on stripe-splitted band components was developed in [ $^{16}$ ]. A model exploiting repulsive (Coulombic plus small electron–phonon) interaction of an itinerant band with a doping-created  $\delta$ -type higher lying state was considered in [ $^{27}$ ].

Recent experimental investigations have yielded more precise and partly unexpected results which need theoretical explanation. The two-component scenario has been supported by measuring the isotope effect also on the paired carrier effective mass (penetration depth), traced to polarons [ $^{10}$ ]. Further, two quasiparticle relaxation times of critical and noncritical behaviour were found [ $^{11}$ ]. In [ $^{26}$ ], the isotope effect of the supercarrier effective mass was looked for using a two-band model and the observed behaviour was revealed (see also [ $^{28}$ ]). In [ $^{29}$ ] it was shown that the presence of a critical and a noncritical relaxation channel is a natural consequence in two-band models.

Recent tunnelling experiments [ $^{30-35}$ ], in accordance with the photoemission studies [ $^{34-36}$ ], have essentially added to reproducible information on excitation spectra and gaps. The one-particle excitation spectrum exhibits a typical peak—dip—hump complex structure. It is considered as a consequence of the opening of the superconducting gap in the electron spectrum and as being of collective origin [ $^{30}$ ]. This feature is regarded as setting several constraints on theoretical models of pairing interaction [ $^{31}$ ]. Recently some theoretical attempts have been made to describe the tunnelling spectra of such type [ $^{37-40}$ ]. Most interesting is the result of [ $^{31,33}$ ] that the gap to  $T_{\rm c}$  ratio  $2\Delta(0)/kT_{\rm c}$ , and even the gap itself is, contrary to  $T_{\rm c}$ , a decreasing function of doping in the "higher" part of the underdoped region. The characteristic ratios mentioned are found to be of non-BCS universality, reaching large values near 10. Theoretically the possibility of a  $2\Delta(0)/\Theta_{\rm c}$  ratio ( $\Theta=kT$ ) diminishing with doping has been already demonstrated in [ $^{23}$ ].

In the present contribution we demonstrate the ability of a very simple two-band model to show the qualitative tendencies mentioned above. This model supposes repulsive interband scattering of intraband pairs between an itinerant band and a narrow distribution of states appearing and expanding with doping at the cost of the number of states of the first band. Taking account also of previous results, it seems that two-band models with doping-dependent electron energy distributions will be able to describe basic superconductivity characteristics in high- $T_{\rm c}$  cuprates. Correspondingly, such models will serve as a way to look for the high- $T_{\rm c}$  mechanism.

#### 2. BASIC FORMULAS

We start with the linearized Hamiltonian of a two-band (a and b) superconductor with the leading interband scattering of the intraband pairs

$$H = \sum_{\vec{k}\sigma} \varepsilon_{a}(\vec{k}) a_{\vec{k}\sigma}^{+} a_{\vec{k}\sigma} + \sum_{\vec{k}\sigma} \varepsilon_{b}(\vec{k}) b_{\vec{k}\sigma}^{+} b_{\vec{k}\sigma}$$

$$+ \sum_{\vec{k}} \Delta_{a}(\vec{k}) \left[ a_{\vec{k}\uparrow} a_{-\vec{k}\downarrow} + a_{-\vec{k}\downarrow}^{+} a_{\vec{k}\uparrow}^{+} \right] - \sum_{\vec{k}} \Delta_{b}(\vec{k}) \left[ b_{\vec{k}\uparrow} b_{-\vec{k}\downarrow} + b_{-\vec{k}\downarrow}^{+} b_{\vec{k}\uparrow}^{+} \right] .$$

$$(1)$$

The order parameters (gaps) are defined as

$$\begin{split} &\Delta_{\mathrm{a}}(\vec{q}) = 2\sum_{\vec{k}} W(\vec{q}, \vec{k}) \langle b_{\vec{k}\uparrow} b_{-\vec{k}\downarrow} \rangle = 2\sum_{\vec{k}} W(\vec{q}, \vec{k}) \langle b_{-\vec{k}\downarrow}^+ b_{\vec{k}\uparrow}^+ \rangle, \\ &\Delta_{\mathrm{b}}(\vec{q}) = 2\sum_{\vec{k}} W(\vec{q}, \vec{k}) \langle a_{-\vec{k}\downarrow} a_{\vec{k}\uparrow} \rangle = 2\sum_{\vec{k}} W(\vec{q}, \vec{k}) \langle a_{\vec{k}\uparrow}^+ a_{-\vec{k}\downarrow}^+ \rangle \;. \end{split} \tag{2}$$

In (1) usual designations are used. The band energies read  $\xi_{\rm a,b}(\vec k)=\varepsilon_{\rm a,b}(\vec k)+\mu$ ,  $\mu$  being the chemical potential. The interaction constant W=U+V characterizing the interband scattering of pairs contains the Coulomb electronic (U) and the electron–phonon part (V), both of which are repulsive. The contribution of interband pairs is omitted with the usual argument of much smaller momentum scattering volume available. Diagonalization of (1) leads to the gap equations

$$\Delta_{\mathbf{a}}(\vec{q}) = \sum_{\vec{k}} W(\vec{q}, \vec{k}) \Delta_{\mathbf{b}}(\vec{k}) E_{\mathbf{b}}^{-1}(\vec{k}) t h \frac{E_{\mathbf{b}}(\vec{k})}{2\Theta},$$

$$\Delta_{\mathbf{b}}(\vec{q}) = \sum_{\vec{k}} W(\vec{q}, \vec{k}) \Delta_{\mathbf{a}}(\vec{k}) E_{\mathbf{a}}^{-1}(\vec{k}) t h \frac{E_{\mathbf{a}}(\vec{k})}{2\Theta}$$
(3)

with the one-particle excitation energies

$$E_{\mathrm{a,b}}(\vec{k}) = \sqrt{\varepsilon_{\mathrm{a,b}}^2(\vec{k}) + \Delta_{\mathrm{a,b}}^2}.$$
 (4)

Two-particle interband excitation energies are determined by  $E_{\rm a} \pm E_{\rm b}$ . The occupation numbers of the renormalized bands per one spin read

$$n_{\rm a,b}(\vec{k}\sigma) = \frac{1}{2} \left[ 1 - \frac{\varepsilon_{\rm a,b}(\vec{k})}{E_{\rm a,b}(\vec{k})} th \frac{E_{\rm a,b}(\vec{k})}{2\Theta} \right]. \tag{5}$$

Supposing further that the lower band (a) is extended in energy from 0 to D with the constant density of states  $\rho_a$  (two-dimensionality of  $\text{CuO}_2$  planes), and the higher band (b) is analogously extended from  $\varepsilon_1$  to  $\varepsilon_2$ , one finds, in the case of wave-vector independent W and gaps, the approximate expression ( $\gamma = e^{0.577}$ ) for the transition temperature:

$$\Theta_{\rm c} = \frac{2\gamma}{\pi} \sqrt{D(\varepsilon_2 - D)} \exp\left\{-\frac{1}{2} \left[ \ln^2 \frac{D}{\varepsilon_2 - D} + \frac{4}{\rho_{\rm a} \rho_{\rm b} W^2} \right]^{1/2} \right\}.$$
 (6)

The  $\Theta_c$  isotope effect exponent is found as

$$\alpha = -C \frac{V}{W} \cdot \frac{1}{W^2 \rho_{\rm a} \rho_{\rm b}} \left[ \ln \frac{\pi}{2\gamma} \frac{\Theta_{\rm c}}{\sqrt{D(\varepsilon_2 - D)}} \right]^{-1} , \qquad (7)$$

where  $C = \mathrm{d} \ln M / \mathrm{d} \ln M_i$  and M is the effective mass of the active vibration, while  $M_i$  is the atomic mass under substitution. Note that for interband interaction  $V \sim M^{-1}$ .

The superconductivity gaps (vanishing simultaneously at  $\Theta_c$ ) at zero temperature are determined from the system

$$|\Delta_{a}(0)| = W \rho_{b} |\Delta_{b}(0)| \ln \frac{\sqrt{(\varepsilon_{2} - D)^{2} + \Delta_{b}(0)^{2}} + \varepsilon_{2} - D}{|\Delta_{b}(0)|},$$

$$|\Delta_{b}(0)| = W \rho_{a} |\Delta_{a}(0)| \ln \frac{\sqrt{D^{2} + \Delta_{a}(0)^{2}} + D}{|\Delta_{a}(0)|}.$$
(8)

Further comments on the scheme used and approximations made can be found in  $[^{21}]$ .

#### 3. THE MODEL AND ILLUSTRATIVE CALCULATIONS

Below we present an interpolative model to describe the two-component scenario and to consider basic dependences of superconductivity characteristics. In quantitative illustrative calculations a reasonable nonspecified set of parameters will be used. Correspondingly, the doping will be characterized by a concentration c, which as a measure can be scaled to a real number of holes introduced into the superconductivity playground.

We suppose that with hole doping over the upper edge of the a-band filled at c=0 a new distribution of electronic states (b-band) will be formed at the equalized cost of a-band states. Let the width of the b-band develop so that  $\varepsilon_2 = D + \nu c^2$  and  $\varepsilon_1 = D$ . Then  $\rho_a = D^{-1}(1-c)$ ,  $\rho_b = (\nu c)^{-1}$  and (with a good accuracy also for  $T < T_c$ )  $\mu = D$ . Correspondingly,

$$\Theta_{\rm c} = 1.14c\sqrt{D\nu} \exp\left\{-\frac{1}{2} \left[\frac{4\nu D}{W^2} \cdot \frac{c}{1-c} + \ln^2 \frac{D}{\nu c^2}\right]^{1/2}\right\}.$$
(9)

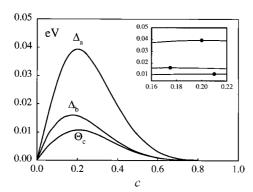
To deal with a system possessing  $T_c$  near 100 K for optimal doping, we choose the following set of parameters:  $D=3, \nu=1, W=0.3$  (eV).

Clearly, the use of wave-vector independent interband coupling and gaps appears as a crude supposition as compared with the established d-wave-dominating nature of the order parameter in high- $T_{\rm c}$  cuprates. However, the results obtained in the framework of the present work seem to be stimulating for further research, which must include  $\vec{k}$ -dependent characteristics connected with the doping-dependent electron spectrum that the authors are not able to introduce at the present. Such a doping dependence can be traced back to strong electronic correlations acting in cuprates.

The behaviour of superconductivity characteristics in the present model is illustrated by Figs. 1–4. The zero-temperature superconductivity gaps  $\Delta_{\rm a,b}(0)$  and the transition-temperature  $T_{\rm c}$  show the usual rise on the way to optimal doping with the following decrease by overdoping (Fig. 1). In connection with the experimental findings discussed in the Introduction, it should be mentioned that the  $\Delta_{\rm a,b}(0)$  maxima are shifted to weaker dopings as compared to  $T_{\rm c}$ .

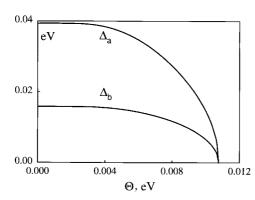
The behaviour of the characteristic ratios  $2\Delta_{a,b}(0)/\Theta_c$  with doping is illustrated in Fig. 2. In the case of the smaller gap (doping-induced band) this ratio diminishes smoothly with doping. This is in agreement with the experiment of  $[^{31-33}]$ . For the other (basic) band  $2\Delta_a(0)/\Theta_c$  possesses a maximum in the region of extended underdoping with the following slow change from diminishing to enhancement. The BCS universality in  $2\Delta_{a,b}(0)/\Theta_c$  is violated and large values near 10 can arise as observed in numerous experiments. The  $\Delta_{a,b}(T)$  dependences are of the usual form (Fig. 3).

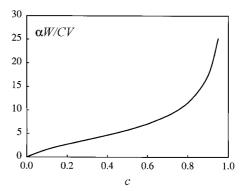
The isotope effect exponent (Fig. 4) rises with doping and is not enhanced for underdoping because of the doping-created nature of the b-band. For the c-independent narrow band submerged in the wider one,  $\alpha$  is enhanced for both under- and overdoped regions where  $T_{\rm c}$  becomes small [ $^{21,22}$ ]. Note that a small percentage of the electron–phonon contribution to the whole interband interaction can lead to remarkable  $\alpha$ -values.



**Fig. 1.** The dependences of the transition temperature and zero temperature gaps on doping for an illustrative set of parameters. In the inset the maxima positions of these quantities are indicated by points.

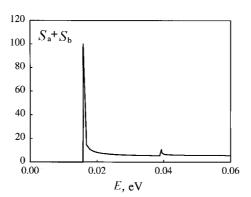
**Fig. 2.** Characteristic zero-temperature gap ratios as functions of doping.





**Fig. 3.** The superconductivity gaps dependent on temperature, c = 0.20.

**Fig. 4.** Transition-temperature isotope exponent vs. doping.



**Fig. 5.** Joint density of one-particle excitations, c = 0.20.

The one-particle densities  $S_{\rm a,b}(E) = \rho_{\rm a,b} E[E^2 - \Delta_{\rm a,b}^2]^{-1/2}$  calculated (without taking account of dispersion, damping, etc.) are of rough guiding nature. However, the characteristic structure of the peak–dip–hump type is recognizable ( $T < T_{\rm c}$ ) in the joint density if one associates the peak with  $\Delta_{\rm b}$  and the hump with  $\Delta_{\rm a}$  (Fig. 5). The spectral feature intensities are determined using  $\rho_{\rm a}/\rho_{\rm b}$ . We mention that arguments given in [ $^{36}$ ] against a two-band interpretation of the peak plus hump feature naturally fail ( $\Delta_{\rm a}=0$  for  $T>T_{\rm c}$ ; interband nature of the interactions). The  $\Delta_{\rm b}$  behaviour is reflected by the peak. In [ $^{36}$ ] it is found that the hump shifts to greater energies with decreasing doping in underdoped samples. Our model exhibits the hump in an extended underdoped region at higher energies with lowering c. Later this behaviour converts to the opposite until the hump becomes hidden in the peak for small c. The temperature approaching  $T_{\rm c}$  quenches the structure under consideration.

A remark must be made concerning the widely expressed statement that the only one Fermi surface observed introduces discrepancies with the two-band models for which two surfaces can be expected. This argument has no formal relevance for the present model because of the doping-independent position of the chemical potential at the energy where the bands touch each other ( $\mu = D$ ). Experimentally there are indications of such a trend at least for some systems (Bi<sub>2</sub>Sr<sub>2</sub>CaCu<sub>2</sub>O<sub>8+ $\delta$ </sub>) [<sup>34,36</sup>].

Further, the observability of two Fermi surfaces is not necessarily dictated by the two bands present. For instance, according to t-J model calculations [41], the narrow and wide bands cross the Fermi surface at nearly the same  $\vec{k}$ , however, their spectral intensities differ markedly. The weaker wide band maximum becomes masked (cf. also Fig. 5 for connected results) and contributes only to the finite spectral intensity at the Fermi surface. A model using  $\mu$  lowering with doping will enable also the description of the pseudogap as a natural excitation threshold of the a-band system in the underdoped region, which transforms with further doping to the usual  $\Delta_a$ .

In conclusion, we note that in spite of all the crude approximations of the model discussed, it can reflect some important dependences and tendencies observed in cuprate high-temperature superconductors. Correspondingly the two-band models remain a channel in which the microscopical mechanism of the high- $T_{\rm c}$  phenomenon can be looked for.

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# KÕRGTEMPERATUURSETE ÜLIJUHTIDE OMADUSED DOPEERIMISEST SÕLTUVA ELEKTRONSPEKTRIGA KAHETSOONILISES MUDELIS

### Nikolai KRISTOFFEL ja Pavel RUBIN

On käsitletud tsoonidevahelise paariülekandega mudelit põhiaine ja dopeeringuga sündival tsoonil (konstantne seisundite koguarv) kirjeldamaks kõrgtemperatuurse ülijuhtivuse kahekomponendilist stsenaariumi. On arvutatud siirdetemperatuuri, isotoopefekti eksponendi ja ülijuhtivuspilude sõltuvus dopeerimisest teooria parameetrite iseloomulikel väärtustel ja saadud aukdopeeringu kasvuga kahanevad pilude suhted siirdetemperatuuri. Üheosakeselises ergastusspektris on identifitseeritav piik–auk–küür-tüüpi kompleks. Vaatamata jämedatele lähendustele peegeldab mudel kupraatülijuhtidel leitud omadusi. Dopeeringust sõltuva elektronspektriga kahetsoonilised mudelid säilitavad koha kõrgtemperatuurse ülijuhtivuse mikromehhanismi tuvastamisel.